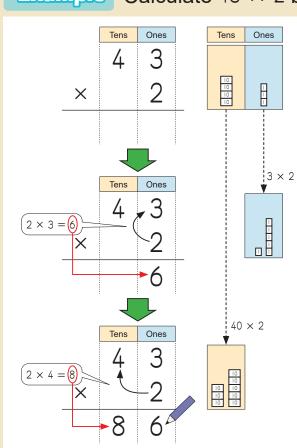
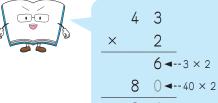
Multiplication Algorithm-

2-Digit Number \times |-Digit Number (\mid)





Line up the numbers vertically in each place.



2 times 3 is 6.

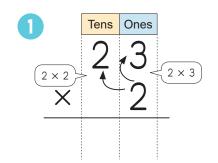
(This is actually $3 \times 2 = 6$.)

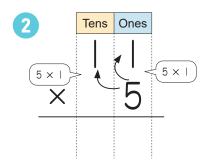
Write a 6 in the ones place.

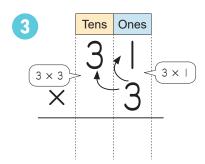
For convenience, the multiplicand and multiplier are reversed!

2 times 4 is 8. (This is actually $40 \times 2 = 80$.) Write a 8 in the tens place.

$$43 \times 2 = 86$$

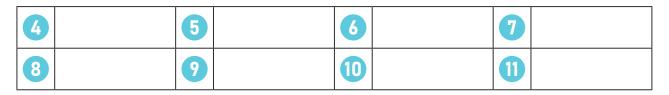






- $\frac{4}{24} \times 2$
- 5 32 × 3
- 6 12 × 4
- 7 21 × 3

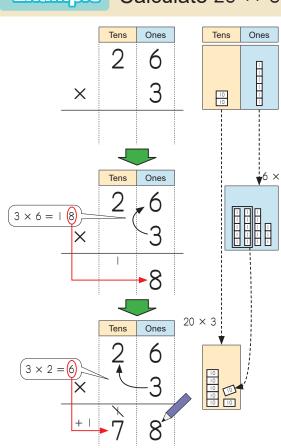
- 8 33 × 3
- 9 42 × 2
- 10 23 × 3
- 34×2



Multiplication Algorithm-

2-Digit Number \times |-Digit Number (2)





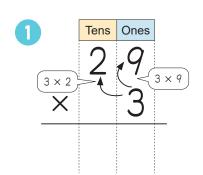
Line up the numbers vertically in each place. 2 6

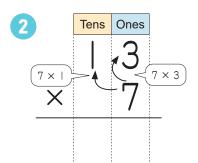
3 times 6 is 18.

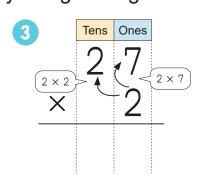
(This is actually $6 \times 3 = 18$.) Write an 8 in the ones place, and regroup | into the tens place.

3 times 2 is 6. (This is actually $20 \times 3 = 60$.) Add the 6 and the | that was regrouped to get 7. Write a 7 in the tens place.

$$26 \times 3 = 78$$







- 4 17 × 5
- $\boxed{5}$ 35 \times 2
- 6 16 × 6
- 723×4

- 8 36 × 2
- 9 28 × 3
- 10 45 imes 2
- 11 12 × 8

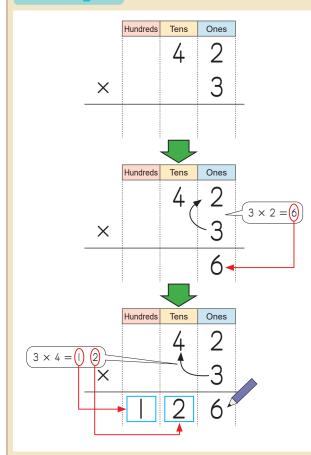
4	5	6	7	
8	9			

Multiplication Algorithm-

2-Digit Number \times |-Digit Number (3)

Example

Calculate 42×3 by using the algorithm.



Line up the numbers vertically in each place.



3 times 2 is 6.

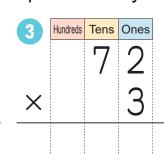
(This is actually $2 \times 3 = 6$.) Write a 6 in the ones place.

3 times 4 is 12. (This is actually $40 \times 3 = 120$.) Write a 2 in the tens place and a | in the hundreds place.

$$42 \times 3 = 126$$

	Hundreds	Tens	Ones
		3	1
	i ! ! ! !		'
X			4

VVIII	9 111	artip	moa	.
2	Hundreds	Tens	Ones	
×		6	3 2	
			_	



4	Hundreds	Tens	Ones
		8	2
×		Ů	4
			•

$$7$$
 4| \times 4

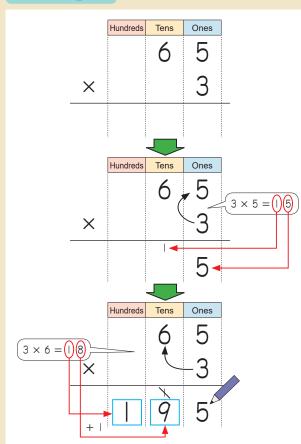
$$32 \times 4$$
 10 52×4

5	6	7	8	
9	10	1	12	

Multiplication Algorithm-

2-Digit Number \times |-Digit Number (4)

Example Calculate 65×3 by using the algorithm.



Line up the numbers vertically in each place.

3 times 5 is |5|. (This is actually $5 \times 3 = |5|$.) Regroup | into the tens place. Write a 5 in the ones place.

3 times 6 is |8|. (This is actually $60 \times 3 = |80|$.) Add the |8| and |4| that was regrouped. It becomes |9|. Write a |9| in the tens place and a |4| in the hundreds place.

$$65 \times 3 = 195$$

- 1 Hundreds Tens Ones 6 4 × 3

- 55 × 6
- 6 38 × 5
- $\sqrt{2}$ 42 × 8
- 8 68 × 7

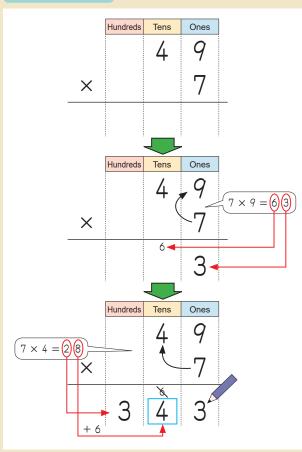
- 9 27 × 6
- $10 78 \times 5$
- 11 93 × 5
- 12 37 × 8

5	6	7	8	
9	10	1	12	

Multiplication Algorithm-

2-Digit Number \times |-Digit Number (5)

Example Calculate 49×7 by using the algorithm.



Line up the numbers vertically in each place.

7 times 9 is 63. (This is actually $9 \times 7 = 63$.) Regroup 6 into the tens place. Write a 3 in the ones place.

7 times 4 is 28. (This is actually $40 \times 7 = 280$.) Add the 28 and the 6 that was regrouped. It becomes 34. Write a 4 in the tens place and a 3 in the hundreds place.

$$49 \times 7 = 343$$

- 5 66 × 8
- 6 89 × 6
- 79 × 9
- 8 36 × 6

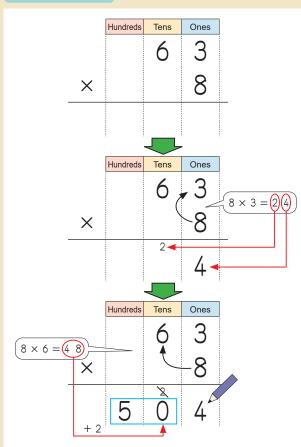
- 9 58 × 9
- 10 47 imes 7
- 11) 68 × 9
- 12 78 × 7

5	6	7	8	
9		•	12	

Multiplication Algorithm-

2-Digit Number × |-Digit Number (6)

Example Calculate 63×8 by using the algorithm.



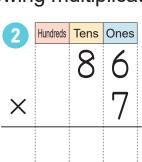
Line up the numbers vertically in each place.

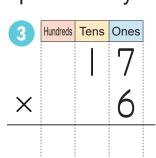
8 times 3 is 24. (This is actually $3 \times 8 = 24$.) Regroup 2 into the tens place. Write a 4 in the ones place.

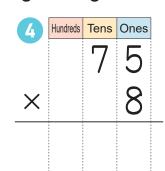
8 times 6 is 48. (This is actually $60 \times 8 = 480$.) Add the 48 and the 2 that was regrouped. It becomes 50. Write a 0 in the tens place and a 5 in the hundreds place.

$$63 \times 8 = 504$$

	Hundreds	Tens	Ones
		7	6
×			4







- 69 × 3
- 75×4
- 8 67 × 9

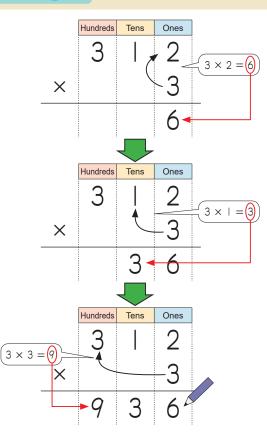
- 9 67 × 3
 - 10 87 × 7
- 11 67 × 6
- $12 77 \times 4$

5	6	7	8	
9	10	1	12	

Multiplication Algorithm-

3-Digit Number × |-Digit Number (□)

Example Calculate 312×3 by using the algorithm.



Line up the numbers vertically in each place. 3 | 2

3 times 2 is 6. (This is actually $2 \times 3 = 6$.) Write a 6 in the ones place.

3 times | is 3 (This is actually $10 \times 3 = 30$.) Write a 3 in the tens place.

3 times 3 is 9 (This is actually $300 \times 3 = 900$.) Write a 9 in the hundreds place.

$$312 \times 3 = 936$$

- 2 Hundreds Tens Ones
 1 2 1

 × 4
- 4 Hundreds Tens Ones
 1 3 2
 × 3

- 5 244 × 2
- 6 123 × 3
- $\sqrt{2}$ 321 \times 2
- 8 221 × 4

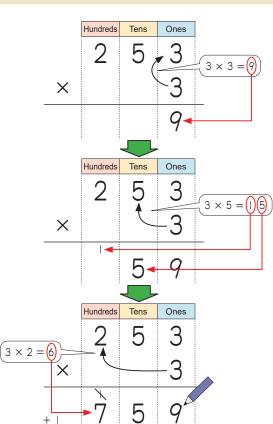
- 9 332 × 3
- $10 143 \times 2$
- 131×2
- 12 213 × 3

5	6	7	8	
9	10	•	12	

Multiplication Algorithm-

3-Digit Number \times |-Digit Number (2)

Example Calculate 253×3 by using the algorithm.



Line up the numbers vertically in each place.

3 times 3 is 9. (This is actually $3 \times 3 = 9$.) Write a 9 in the ones place.

3 times 5 is |5|. (This is actually $50 \times 3 = |50|$.) Regroup | into the hundreds place. Write a 5 in the tens place.

3 times 2 is 6. (This is actually $200 \times 3 = 600$.) Add the 6 and the | that was regrouped. It becomes 7. Write a 7 in the hundreds place.

$$253 \times 3 = 759$$

- 1 Hundreds Tens Ones 2 6 3 × 3

- 5 492 × 2
- $6 242 \times 4$
- $\sqrt{1}$ 172 × 3
- 8 |4| × 6

- 9 364 × 2
- $10 273 \times 3$
- 11 461 × 2
- 12 392 × 2

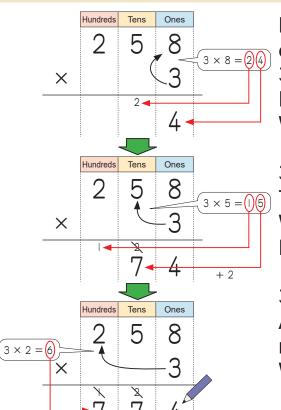


Multiplication Algorithm-

3-Digit Number × |-Digit Number (3)

Example

Calculate 258×3 by using the algorithm.



Line up the numbers vertically in each place.

3 times 8 is 24.

Regroup 2 into the tens place. Write a 4 in the ones place.

3 times 5 is 15.

The regrouped 2 and 5 make 7. Write a 7 in the tens place.

Regroup | into the hundreds place.

3 times 2 is 6.

Add the 6 and the 1 that was regrouped. It becomes 7. Write a 7 in the hundreds place.

$$258 \times 3 = 774$$

- Hundreds Tens Ones 4 8 X
- Hundreds Tens Ones 3 5 X
- Hundreds Tens Ones 6 X
- Hundreds Tens Ones 8 4 X

- 298×2
- 144×6
- 153×5
- 297×3

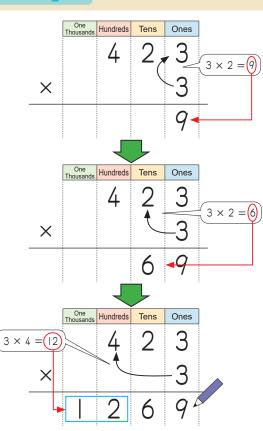
- 134×7
- 10 234×4
- M 164×6
- 12 289×2

5	6	7	8	
9	10	•	12	

Multiplication Algorithm-

3-Digit Number × |-Digit Number (4)

Example Calculate 423×3 by using the algorithm.



Line up the numbers vertically in each place.

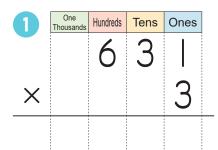
3 times 3 is 9. Write a 9 in the ones place.

3 times 2 is 6. Write a 6 in the tens place.

3 times 4 is |2. Regroup | into the one thousands place.

Write a 2 in the hundreds place and a | in the one thousands place.

$$428 \times 3 = 1269$$



2	One Thousands	Hundreds	Tens	Ones
		7	4	3
X				2

3	One Thousands	Hundreds	Tens	Ones
		5	2	3
×			_	ر ح
				J

$$\frac{1}{1}$$
 412 × 4

$$8711 \times 7$$

$$11$$
 723 × 3

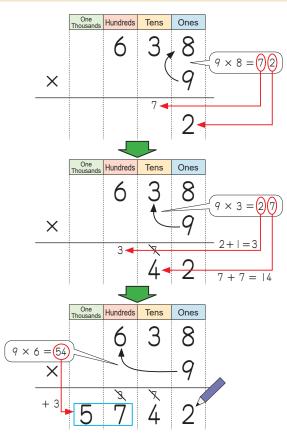
4	5	6	7	
8	9		1	

Multiplication Algorithm-

3-Digit Number \times |-Digit Number (5)

Example

Calculate 638×9 by using the algorithm.



Line up the numbers vertically in each place.

9 times 8 is 72.

Write a 2 in the ones place.

Regroup 7 into the tens place.

9 times 3 is 27.

The regrouped 7 and 7 make | 4.

Write a 4 in the tens place and regroup | into the hundreds place.

The regrouped | and 2 make 3.

Regroup 3 into the hundreds place.

9 times 6 is 54.

The regrouped 3 and 4 make 7.

Write a 7 in the hundreds place.

Regroup | into the one thousands place.

Write a 2 in the hundreds place and a | in the one thousands place.

 $638 \times 9 = 5742$



	_			
2	One Thousands	Hundreds	Tens	Ones
		7	5	2
×				7

3	One Thousands	Hundreds	Tens	Ones
		4	6	3
×		'		8

4	378	×	4
4	378	X	4

$$5 472 \times 7$$

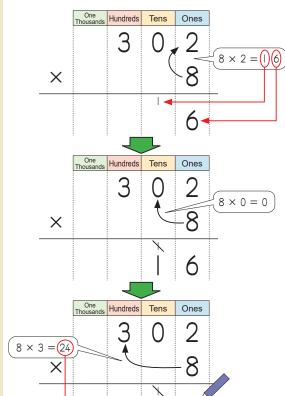
$$11$$
 346 × 7

4	5	6	0
8	9	10	1

Multiplication Algorithm-

3-Digit Number \times 1-Digit Number (6)

Example Calculate 302×8 by using the algorithm.



Line up the numbers vertically in each place.

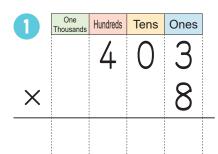
8 times 2 is 16.
Write a 6 in the ones place.
Regroup 1 into the tens place.

8 times 0 is 0.
The regrouped | and 0 make |.
Write a | in the tens place.

8 times 3 is 24.
Write a 4 in the hundreds place.
Regroup 2 into the one thousands place.
Write a 2 in the one thousands place.

Write a 2 in the one thousands place.

$$302 \times 8 = 2416$$



2	One Thousands	Hundreds	Tens	Ones
		6	0	8
X				7

3	One Thousands	Hundreds	Tens	Ones
		7	0	9
X		·		6

4	5	6	7	
8	9	10	1	

Multiplication Algorithm-

Properties of Multiplication

Devise a way to calculate the following multiplication problem and then calculate it.

$$75 \times 5 \times 2 = \boxed{75 \times (5 \times 2) = 75 \times 10 = 750}$$

If you calculate 5×2 first, it becomes $| 0 \rangle$. Then it is easier to calculate $75 \times | 0 \rangle$.



When you multiply 3 numbers, whether you start by calculating the first 2 numbers or the last 2 numbers, the answer is the same.

Devise a way to calculate the following multiplication problems and then calculate them.

$$5 102 \times 2 \times 3 =$$

$$6 125 \times 2 \times 5 =$$

$$9$$
 328 \times 5 \times 2 =

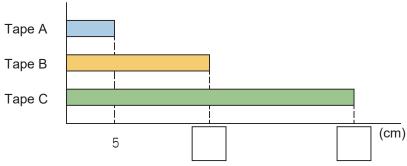
Try to find the easiest way to calculate these! You can calculate the last 2 numbers first, so it is easier to solve.



Multiplication Algorithm-

Calculation with Times as Much

There are 3 tapes. The length of tape A is 5 cm. **Example** The length of tape B is 3 times as long as tape A. The length of tape C is 2 times as long as tape B. How long are tapes B and C?



Calculate the length of tape B.

 $5 \times 3 = 15$ Tape B is 15 cm Calculate the length of tape C.

 $15 \times 2 = 30$ Tape C is 30 cm

Tape C Tape B 15 30 cm Answer

There are 3 ropes. The length of rope A is 80 cm. The length of rope B is 3 times as long as rope A. The length of rope C is 2 times as long as rope B. How long are ropes B and C?

> Rope B Rope C Answer cm cm

- 2 There are 3 boxes with oranges. There are 20 oranges in box A. The number of oranges in box B is 2 times as many as box
 - A. The number of oranges in box C is 3 times as many as box
 - B. How many oranges are there in boxes B and C?

oranges in box B, oranges in box C Answer

(0) - 15

Multiplication Algorithm-1

Review

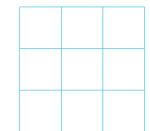
Calculate these multiplication problems by using the algorithm.

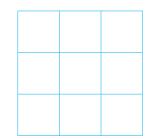
 41×2

 12×3

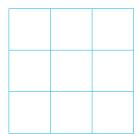
3 21×2 25×3

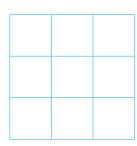


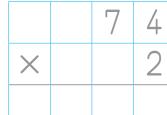


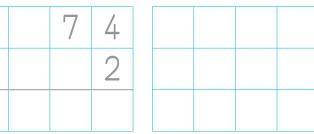


- 38×2
- 6 16 × 4
- 74×2
- 93×3









Calculate these multiplication problems by using the algorithm.

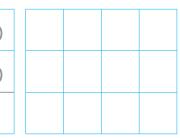
56 × 6

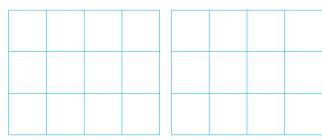
 39×5

 69×8

 78×8





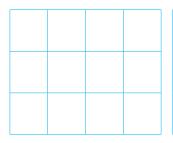


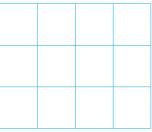
68 × 3

 26×4

 36×3

8 25×4









Calculate these multiplication problems by using the algorithm.

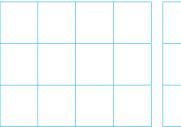
 243×2

 261×3

 231×4

 142×6





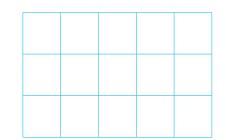




 753×7



 309×8



- Devise a way to calculate the following multiplication problems and then calculate them.
- $90 \times 4 \times 2 =$
- $60 \times 3 \times 3 =$
- $253 \times 2 \times 5 =$
- $87 \times 5 \times 2 =$
- There are 3 wooden sticks. The length of stick A is 60 cm. The length of stick B is 3 times as long as stick A. The length of stick C is 2 times as long as stick B. How long are sticks B and C?

stick B stick C Answer cm cm