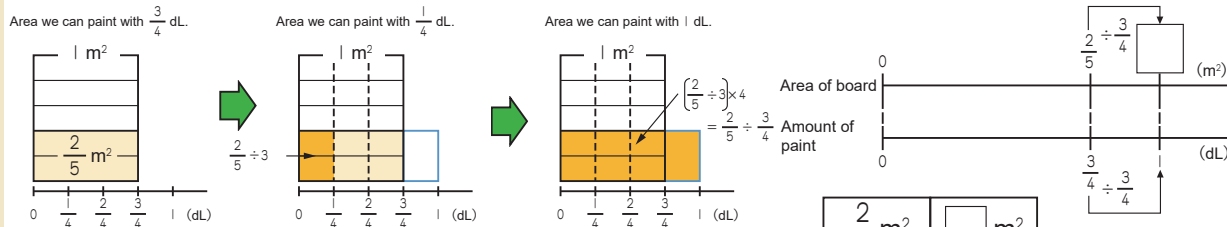


5 - 1

How to Divide by Fractions

Dividing by Fractions (1)

Example $\frac{2}{5}$ m² can be covered with $\frac{3}{4}$ dL of paint. How much area can be covered with 1 dL of paint?



Math sentence

$$\frac{2}{5} \div \frac{3}{4}$$



How can we calculate this?
We have two ways.

$\frac{2}{5}$ m ²	<input type="text"/> m ²
$\frac{3}{4}$ dL	1 dL

Calculating by converting the divisor into 1 means that we multiply the dividend by the reciprocal of the divisor.

Calculate by converting the divisor into a whole number

$$\begin{aligned} &= \left(\frac{2}{5} \times 4 \right) \div \left(\frac{3}{4} \times 4 \right) = \left(\frac{2}{5} \times 4 \right) \div 3 \\ &= \frac{2 \times 4}{5} \div 3 = \frac{2 \times 4}{5 \times 3} = \frac{8}{15} \end{aligned}$$

Calculate by converting the divisor into 1

$$\begin{aligned} &= \left(\frac{2}{5} \times \frac{4}{3} \right) \div \left(\frac{3}{4} \times \frac{4}{3} \right) \\ &= \frac{2}{5} \times \frac{4}{3} = \frac{8}{15} \end{aligned}$$

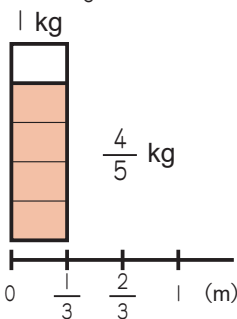
Answer $\frac{8}{15}$ m²

To divide by a fraction, we can multiply the dividend by the reciprocal of the divisor.

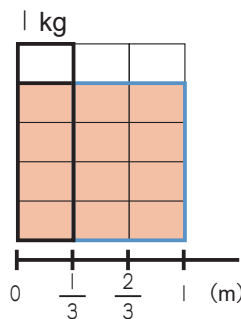
$$\frac{b}{a} \div \frac{d}{c} = \frac{b}{a} \times \frac{c}{d} = \frac{b \times c}{a \times d}$$

1 $\frac{1}{3}$ m of lumber weighs $\frac{4}{5}$ kg. How much does 1 m of lumber weigh?

Weight with $\frac{1}{3}$ m of lumber.

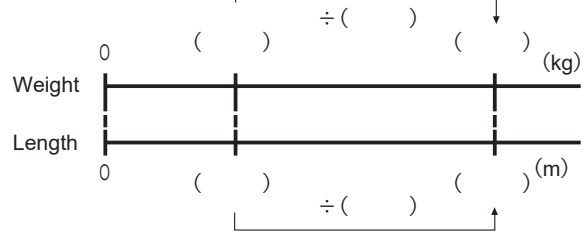


Weight with 1 m of lumber.



Complete the number line diagrams and tables.

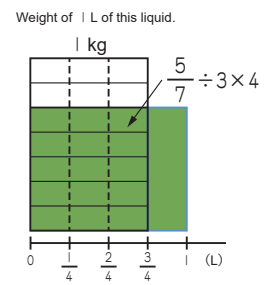
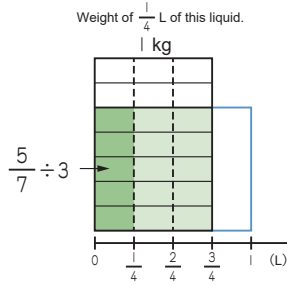
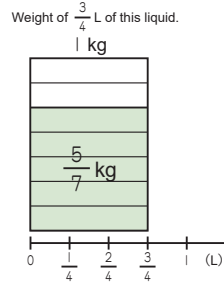
() kg	() kg
() m	() m



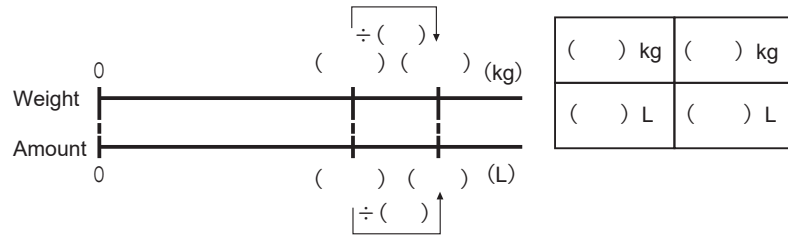
Math sentence

Answer

2 There is a $\frac{3}{4}$ L liquid that weighs $\frac{5}{7}$ kg. How much is 1 L of this liquid weighs?

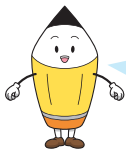


Math sentence

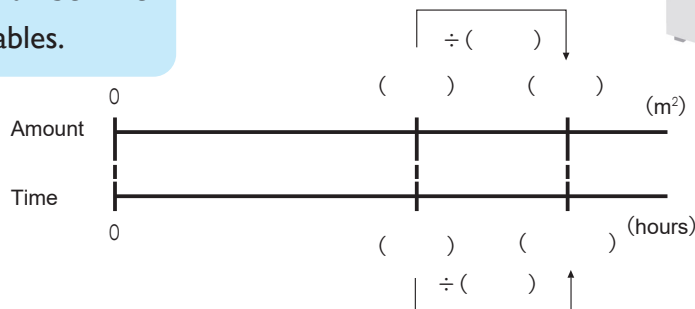


Answer

3 A printer takes $\frac{1}{6}$ of an hour to print $\frac{2}{7}$ m² of paper. How many m² of Paper can be printed in 1 hour?



Complete the number line diagrams and tables.



Math sentence

() m ²	() m ²
() of an hour	() hour

Answer

4 Calculate the following division problems. Simplify the answers when possible. Leave the answers as improper fractions.

1 $\frac{3}{8} \div \frac{2}{7} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

2 $\frac{2}{5} \div \frac{1}{4} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

3 $\frac{5}{6} \div \frac{3}{7}$

4 $\frac{1}{3} \div \frac{2}{5}$

5 $\frac{4}{3} \div \frac{5}{2}$

6 $\frac{4}{5} \div \frac{9}{8}$

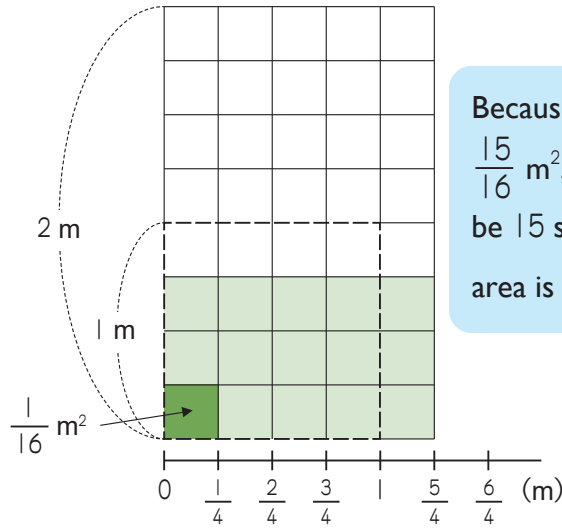
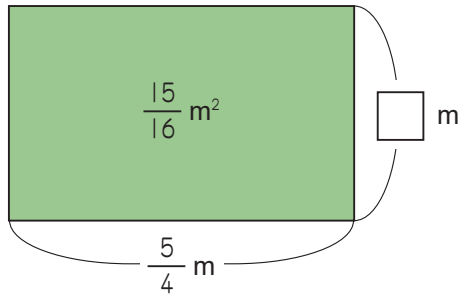
5 - 2

How to Divide by Fractions

Dividing by Fractions (2)

Example 1

A rectangle with an area of $\frac{15}{16} \text{ m}^2$ has a length of $\frac{5}{4} \text{ m}$.
What is the width of the rectangle?



Because the area is $\frac{15}{16} \text{ m}^2$, there should be 15 squares whose area is $\frac{1}{16} \text{ m}^2$.

Math sentence

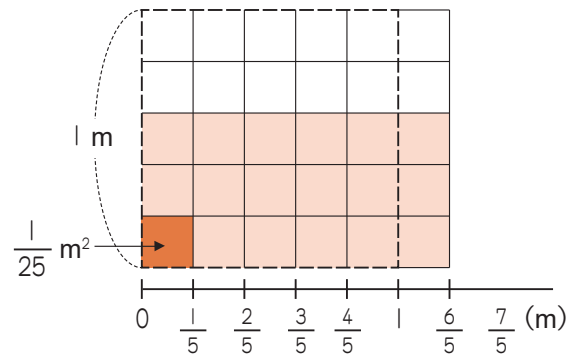
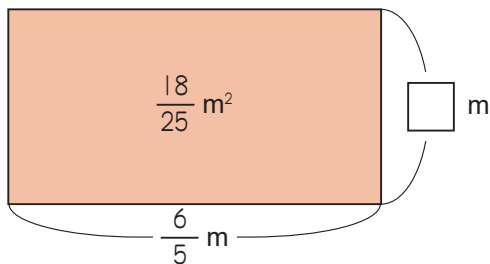
$$\begin{aligned} \frac{15}{16} \div \frac{5}{4} &= \frac{15}{16} \times \frac{4}{5} \\ &= \frac{\overset{3}{\cancel{15}} \times \overset{1}{\cancel{4}}}{\underset{4}{\cancel{16}} \times \underset{1}{\cancel{5}}} = \boxed{\frac{3}{4}} \end{aligned}$$

Answer $\frac{3}{4} \text{ m}$

Rewrite the division math sentence as multiplying by the divisor's reciprocal. Simplify by finding the greatest common factor before multiplying.

1 A rectangle with an area of $\frac{18}{25} \text{ m}^2$ has a length of $\frac{6}{5} \text{ m}$.

What is the width of the rectangle?



Math sentence

Answer

Example 2

I have $\frac{5}{6}$ L of milk. If I drink $\frac{5}{24}$ L of milk every day, how many days worth of milk do I have?

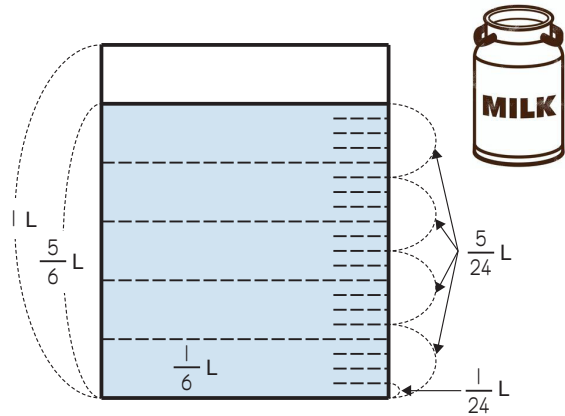
Math sentence

$$\frac{5}{6} \div \frac{5}{24} = \frac{5}{6} \times \frac{24}{5} = \frac{\overset{1}{\cancel{5}} \times \overset{4}{\cancel{24}}}{\underset{1}{\cancel{6}} \times \underset{1}{\cancel{5}}} = 4$$



Answer 4 days

If this problem uses the whole numbers, such as “I have 10 L of milk and I drink 2 L every day,” we can make a math sentence easily.



2 Our office has $\frac{25}{3}$ L of gasoline. If we use $\frac{5}{6}$ L of gasoline every day, how many days worth of gasoline our office have?

Math sentence



Answer _____

3 Calculate the following division problems. Simplify the answers when possible. Leave the answers as improper fractions.

1 $\frac{6}{7} \div \frac{3}{5} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

2 $\frac{9}{10} \div \frac{4}{5} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

3 $\frac{12}{5} \div \frac{8}{15}$

4 $\frac{7}{6} \div \frac{21}{8}$

5 $\frac{3}{8} \div \frac{9}{14}$

6 $\frac{2}{15} \div \frac{6}{5}$

7 $\frac{4}{15} \div \frac{2}{9}$

8 $\frac{14}{15} \div \frac{7}{12}$

5 - 3

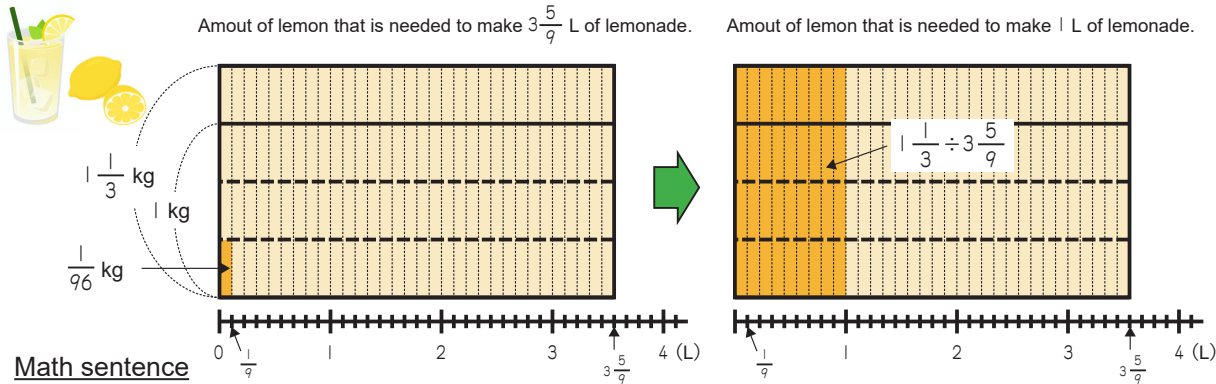
How to Divide by Fractions

Dividing Mixed Numbers by Mixed Numbers

Example

$1 \frac{1}{3}$ kg of lemons are needed to make $3 \frac{5}{9}$ L of lemonade.

How many kg of lemons are needed to make we need to make 1 L of lemonade?

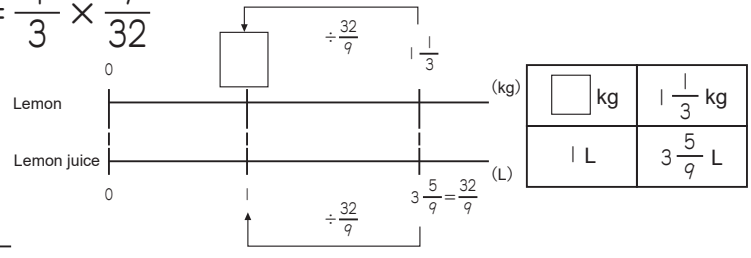


Math sentence

$$1 \frac{1}{3} \div 3 \frac{5}{9} = \frac{4}{3} \div \frac{32}{9} = \frac{4}{3} \times \frac{9}{32}$$

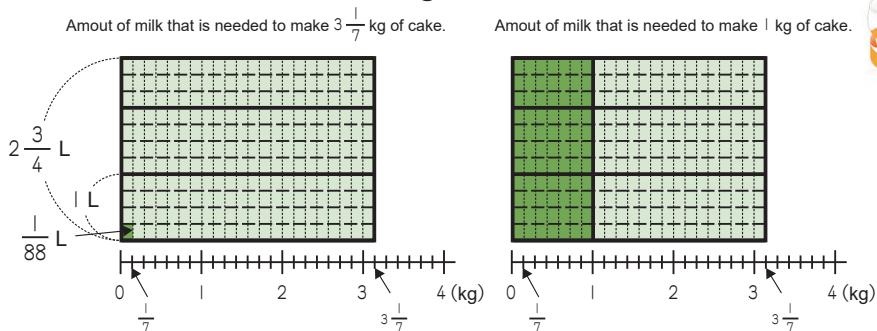
$$= \frac{\cancel{4} \times \cancel{9}^3}{3 \times \cancel{32}_8} = \frac{3}{8}$$

Answer $\frac{3}{8}$ kg



Divide a mixed number by a mixed number: (a mixed number) ÷ (a mixed number)
Change both mixed numbers to improper fractions then divide.

1 $2 \frac{3}{4}$ L of milk is needed to bake a $3 \frac{1}{7}$ kg cake. How much milk is needed to bake a 1 kg cake?



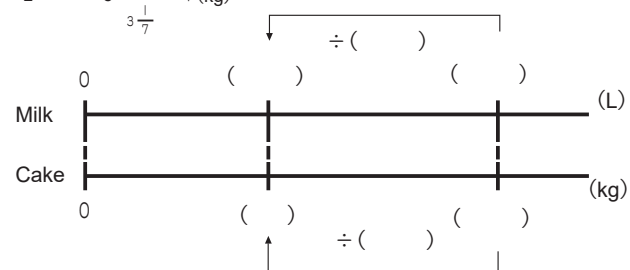
Math sentence

Answer _____



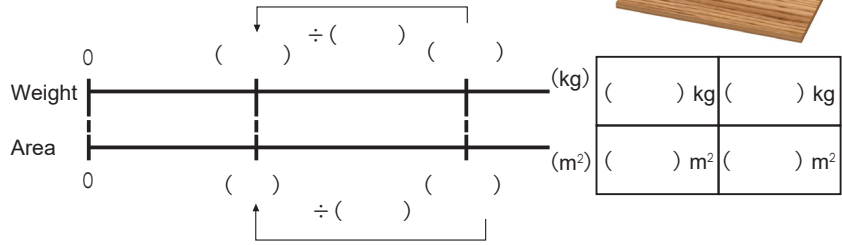
Complete the number line diagrams and tables.

() kg	() kg
() L	() L



2 There is a plywood that is $4\frac{1}{6}$ m² and $5\frac{5}{8}$ kg. If we cut out a 1 m² from this plywood, how much does it weigh?

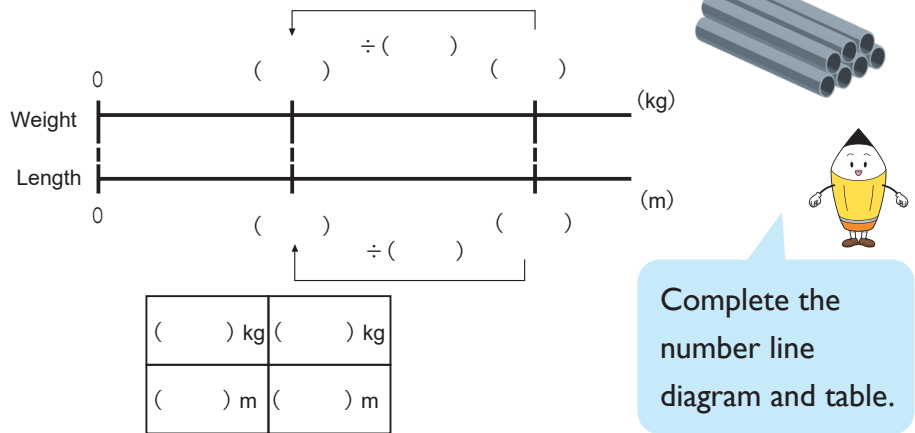
Math sentence



Answer

3 A $8\frac{1}{3}$ m metal pipe weighs $11\frac{1}{9}$ kg. How much does 1 m of this pipe weigh?

Math sentence



Complete the number line diagram and table.

Answer

4 Calculate the following division problems. Simplify the answers. If the answer is an improper fraction, change it to a mixed number.

1 $1\frac{3}{5} \div 2\frac{1}{3} = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$ **2** $1\frac{4}{5} \div 2\frac{1}{2} = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

3 $3\frac{1}{3} \div 1\frac{7}{9}$ **4** $1\frac{5}{9} \div 1\frac{1}{6}$

5 $4\frac{1}{2} \div 3\frac{3}{4}$ **6** $1\frac{1}{9} \div 7\frac{1}{2}$

7 $3\frac{1}{5} \div 1\frac{5}{7}$ **8** $1\frac{1}{2} \div 1\frac{1}{8}$

5 - 4

How to Divide by Fractions

Dividing with Whole Numbers and Fractions

Example 1 Calculate $2 \div \frac{3}{7}$

Remember, 2 can also be written as $\frac{2}{1}$.



$$2 \div \frac{3}{7} = \frac{2}{1} \div \frac{3}{7} = \frac{2}{1} \times \frac{7}{3} = \frac{2 \times 7}{1 \times 3} = \frac{14}{3}$$



Simplify the answers. But you can leave them as improper fractions.

1 Calculate the following division problems.

1 $6 \div \frac{5}{7} = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

2 $4 \div \frac{9}{2} = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

3 $15 \div \frac{10}{3}$

4 $8 \div \frac{6}{5}$

5 $9 \div \frac{12}{7}$

6 $16 \div \frac{24}{5}$

7 $20 \div 1 \frac{3}{7}$

8 $12 \div 1 \frac{1}{3}$

Example 2 Calculate $\frac{3}{7} \div 2$

The whole number 2 can be written as $\frac{2}{1}$. Its reciprocal is $\frac{1}{2}$.



$$\frac{3}{7} \div 2 = \frac{3}{7} \div \frac{2}{1} = \frac{3}{7} \times \frac{1}{2} = \frac{3 \times 1}{7 \times 2} = \frac{3}{14}$$

2 Calculate the following division problems.

1 $\frac{7}{8} \div 4 = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

2 $\frac{1}{2} \div 3 = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

3 $\frac{5}{7} \div 10$

4 $\frac{8}{9} \div 2$

5 $\frac{20}{3} \div 8$

6 $5 \frac{1}{3} \div 6$

5 - 5

How to Divide by Fractions

Dividing Decimal Numbers by Fractions

Example Calculate $0.7 \div \frac{2}{3}$



First change the decimal number to a fraction.

Remember, 0.7 is also “seven tenths” or $\frac{7}{10}$.

$$0.7 \div \frac{2}{3} = \frac{7}{10} \div \frac{2}{3} = \frac{7 \times 3}{10 \times 2} = \frac{21}{20}$$

1 Calculate the following multiplication problems. Simplify the answers. Leave the answers as improper fractions.

1 $0.3 \div \frac{2}{7} = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

2 $0.1 \div \frac{2}{3} = \frac{\square}{\square} \div \frac{\square}{\square} = \frac{\square}{\square} \times \frac{\square}{\square} = \frac{\square}{\square}$

3 $0.9 \div \frac{1}{2}$

4 $0.5 \div \frac{3}{2}$

5 $2.7 \div \frac{3}{5}$

6 $1.5 \div 2 \frac{1}{7}$

7 $0.2 \div 1 \frac{1}{8}$

8 $0.9 \div 3 \frac{3}{5}$

2 Explain the following calculation errors and calculate them correctly.

1 $4.6 \div 3 \frac{5}{6} = \frac{46}{10} \div \frac{23}{6} = \frac{46}{10} \times \frac{23}{\cancel{6}_3} = \frac{529}{30}$

2 $1.8 \div \frac{6}{5} = \frac{18}{100} \div \frac{6}{5} = \frac{\cancel{18}_3}{100} \times \frac{\cancel{5}_1}{\cancel{6}_2} = \frac{3}{20}$

5 - 6

How to Divide by Fractions

Multiplying and Dividing by Fractions (1)

Example Calculate $\frac{5}{6} \times \frac{3}{10} \div \frac{4}{9}$



To divide a fraction, multiply by its reciprocal. Simplify fractions by finding the greatest common factor. Multiply all numerators to equal the answer's numerator. Multiply all denominators to equal the answer's denominator.

$$\begin{aligned} \frac{5}{6} \times \frac{3}{10} \div \frac{4}{9} &= \frac{5}{6} \times \frac{3}{10} \times \frac{9}{4} \\ &= \frac{\overset{1}{\cancel{5}} \times \overset{1}{\cancel{3}} \times 9}{\underset{2}{\cancel{6}} \times \underset{2}{\cancel{10}} \times 4} = \frac{9}{16} \end{aligned}$$

1 Calculate the following. Simplify the answers. Leave them as improper fractions.

1 $\frac{1}{6} \times \frac{2}{3} \div \frac{2}{5}$

2 $\frac{1}{2} \times \frac{9}{2} \div \frac{3}{10}$

3 $\frac{7}{3} \times \frac{5}{9} \div \frac{10}{3}$

4 $\frac{1}{4} \times \frac{6}{5} \div \frac{9}{5}$

5 $\frac{9}{4} \times \frac{5}{2} \div \frac{7}{8}$

6 $\frac{2}{5} \times \frac{3}{4} \div \frac{7}{10}$

7 $\frac{5}{6} \times \frac{2}{15} \div \frac{5}{3}$

8 $\frac{12}{7} \times \frac{2}{3} \div \frac{8}{9}$

2 Explain the following calculation errors and calculate them correctly.

1 $\frac{5}{6} + \frac{2}{3} = \frac{5+2}{6+3} = \frac{7}{9}$

2 $\frac{3}{2} \times \frac{1}{3} \div \frac{3}{4} = \frac{\overset{1}{\cancel{3}}}{2} \times \frac{1}{\underset{1}{\cancel{3}}} \times \frac{3}{4} = \frac{3}{8}$



Remember the previous learning?

5 - 7

How to Divide by Fractions

Multiplying and Dividing by Fractions (2)

Example Calculate $\frac{5}{9} \div \frac{7}{8} \times \frac{3}{4}$



Remember, to divide by a fraction, multiply by its reciprocal. Simplify fractions by finding the greatest common factor. Multiply all denominators to equal to the answer's denominator.

$$\begin{aligned} \frac{5}{9} \div \frac{7}{8} \times \frac{3}{4} &= \frac{5}{9} \times \frac{8}{7} \times \frac{3}{4} \\ &= \frac{5 \times \overset{2}{\cancel{8}} \times \overset{1}{\cancel{3}}}{\underset{3}{\cancel{9}} \times 7 \times \underset{1}{\cancel{4}}} = \frac{10}{21} \end{aligned}$$

1 Calculate the following. Simplify the answers. Leave them as improper fractions.

1 $\frac{1}{5} \div \frac{1}{3} \times \frac{6}{7}$

2 $\frac{2}{3} \div \frac{8}{9} \times \frac{3}{4}$

3 $\frac{3}{8} \div \frac{5}{6} \times \frac{2}{9}$

4 $\frac{4}{5} \div \frac{3}{4} \times \frac{9}{8}$

5 $\frac{1}{5} \div \frac{2}{3} \times \frac{5}{6}$

6 $\frac{1}{2} \div \frac{1}{4} \times \frac{1}{3}$

7 $\frac{6}{7} \div \frac{5}{6} \times \frac{7}{8}$

8 $\frac{3}{4} \div \frac{2}{5} \times \frac{8}{9}$

2 Explain the following calculation errors and calculate them correctly.

1 $\frac{7}{6} - \frac{3}{7} = \frac{\overset{1}{\cancel{7}}}{\underset{2}{\cancel{6}}} - \frac{\overset{1}{\cancel{3}}}{\underset{1}{\cancel{7}}} = \frac{1}{2}$

2 $\frac{\overset{1}{\cancel{5}}}{7} \div \frac{9}{\underset{2}{\cancel{10}}} = \frac{1}{7} \times \frac{2}{9} = \frac{2}{63}$



Remember the previous learning?

5 - 8

How to Divide by Fractions

Dividing by More than One Fraction

Example Calculate $\frac{1}{3} \div \frac{1}{4} \div \frac{1}{6}$



$$\frac{1}{3} \div \frac{1}{4} \div \frac{1}{6} = \frac{1}{3} \times \frac{4}{1} \times \frac{6}{1}$$

$$= \frac{1 \times 4 \times \overset{2}{\cancel{6}}}{\underset{1}{\cancel{3}} \times 1 \times 1} = \frac{8}{1} = 8$$

Sometimes there is more than one division in a math sentence. For each division by a fraction, multiply by its reciprocal.

Calculate the following. Simplify the answers. Leave them as improper fractions.

1 $\frac{5}{9} \div \frac{5}{6} \div \frac{3}{7}$

2 $\frac{3}{4} \div \frac{9}{5} \div \frac{5}{8}$

3 $\frac{2}{3} \div \frac{8}{7} \div \frac{2}{9}$

4 $\frac{5}{6} \div \frac{6}{7} \div \frac{7}{8}$

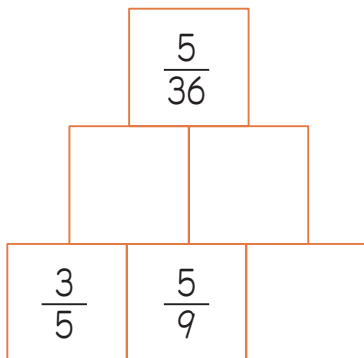
5 $\frac{1}{2} \div \frac{5}{6} \div \frac{9}{10}$

6 $\frac{1}{8} \div \frac{2}{9} \div \frac{3}{10}$

7 $\frac{4}{5} \div \frac{8}{7} \div \frac{14}{15}$

8 $\frac{2}{3} \div \frac{3}{4} \div \frac{4}{5}$

Let's Try !



Multiply the horizontal fractions and write the answer in the above.

We have to calculate not only by multiplying fractions, but also by dividing fractions.

Give a hint to those who are wondering where to calculate. You can do it from the on the left of the second row.



5 - 9

How to Divide by Fractions

Dividing by Decimal Numbers and by Fractions

Example Calculate $1.5 \div \frac{3}{2} \div 3$



$$1.5 \div \frac{3}{2} \div 3 = \frac{15}{10} \times \frac{2}{3} \times \frac{1}{3}$$

$$= \frac{\overset{3}{\cancel{15}} \times \overset{1}{\cancel{2}} \times 1}{\underset{2}{\cancel{10}} \times \underset{1}{\cancel{3}} \times 3} = \frac{1}{3}$$

Change decimal numbers to fractions. Change mixed numbers to improper fractions. Divide fractions by multiplying by its reciprocal. Simply when possible.

Calculate the following. Simply the answers. Leave them as improper fractions.

1 $0.4 \div \frac{4}{7} \div 14$

2 $0.6 \div \frac{1}{2} \div 3$

3 $1.8 \div \frac{1}{2} \div 9$

4 $1.5 \div \frac{1}{8} \div 5$

5 $2.4 \div \frac{3}{5} \div 3$

6 $3.6 \div \frac{6}{7} \div 14$

7 $2.7 \div \frac{9}{10} \div 7$

8 $5 \div \frac{15}{2} \div 0.5$

Let's Try !

Put the three numbers, 2, 3, and 6 in the following to complete the math sentence. We can use each number only one time.

$$\frac{\square}{\square} \div \frac{1}{\square} = \frac{4}{7}$$

Let's try various cases and find the correct answer.

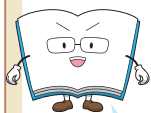


5 - 10

How to Divide by Fractions

Division and Multiplication with Various Kinds of Numbers

Example Calculate $6 \times \frac{8}{5} \div 2.1$



$$6 \times \frac{8}{5} \div 2.1 = \frac{6}{1} \times \frac{8}{5} \div \frac{21}{10} = \frac{6}{1} \times \frac{8}{5} \times \frac{10}{21}$$

$$= \frac{\overset{2}{\cancel{6}} \times 8 \times \overset{2}{\cancel{10}}}{1 \times \underset{1}{\cancel{5}} \times \underset{7}{\cancel{21}}} = \frac{32}{7}$$

Remember to change whole numbers and decimal numbers to fractions. Divide by multiplying by a fraction's reciprocal. Simplify by dividing a numerator and a denominator by its greatest common factor.

Calculate the following. Simplify the answers. Leave them as improper fractions.

1 $2 \times \frac{1}{5} \div 0.6$

2 $3 \times \frac{1}{6} \div 0.9$

3 $9 \times \frac{2}{3} \div 1.6$

4 $5 \times \frac{3}{8} \div 1.5$

5 $0.2 \times \frac{7}{8} \div 2.8$

6 $0.4 \times \frac{4}{5} \div 1.6$

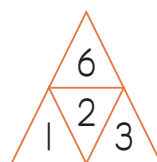
7 $0.8 \times \frac{2}{5} \div 0.06$

8 $0.6 \times \frac{1}{25} \div 0.01$

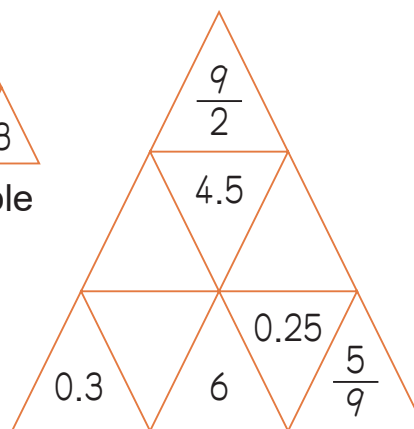
Let's Try !

As the example, multiply the three numbers side by side and write the answer in the above \triangle .

Complete a number pyramid.



Example



We have to calculate not only by multiplying fractions, but also by dividing fractions.



5 - 11

How to Divide by Fractions

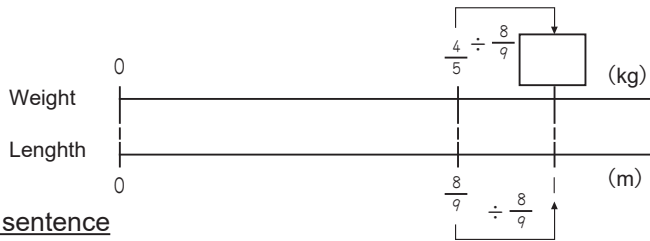
Division Problems

Example An $\frac{8}{9}$ m long iron bar weighs $\frac{4}{5}$ kg.

1 How much does 1 m of this iron bar weigh?

2 How long is 1 kg of this bar?

1



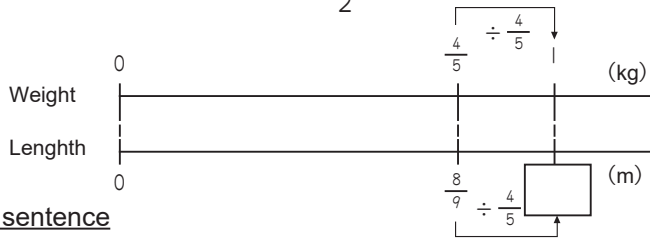
$\frac{4}{5}$ kg	<input type="text"/> kg
$\frac{8}{9}$ m	1 m

Math sentence

$$\begin{array}{l} \text{weight length} \\ \frac{4}{5} \div \frac{8}{9} = \frac{\cancel{4}^1}{5} \times \frac{9}{\cancel{8}_2} = \frac{9}{10} \end{array}$$

Answer $\frac{9}{10}$ kg

2



$\frac{4}{5}$ kg	1 kg
$\frac{8}{9}$ m	<input type="text"/> m

Math sentence

$$\begin{array}{l} \text{length weight} \\ \frac{8}{9} \div \frac{4}{5} = \frac{\cancel{8}^2}{9} \times \frac{5}{\cancel{4}_1} = \frac{10}{9} \text{ or } 1 \frac{1}{9} \end{array}$$

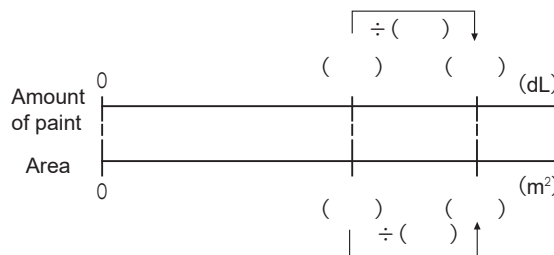
Answer $\frac{10}{9}$ m or $1 \frac{1}{9}$ m

The calculation will change depending on which amount is used as the standard.

A carpenter can paint $\frac{2}{3}$ m² of a wall with $\frac{4}{7}$ dL of paint.

1 How many dL of paint does he need to paint 1 m² of the wall?

Math sentence



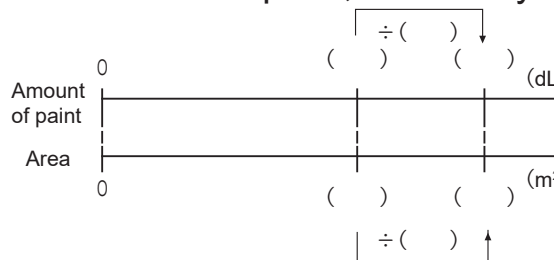
() dL	() dL
() m ²	() m ²

Answer _____

Complete the number line diagram and table.

2 If the carpenter has 1 dL of paint, how many m² of the wall can he paint?

Math sentence



() dL	() dL
() m ²	() m ²

Answer _____

5 - 12

How to Divide by Fractions

Size of the Product

Instruction

In multiplication, when the multiplier is a whole number or decimal number, the size of the product and the size of the multiplicand are related in the following pattern:

- ① When multiplier > 1 , product $>$ multiplicand
- ② When multiplier < 1 , product $<$ multiplicand
- ③ When multiplier $= 1$, product $=$ multiplicand

For example, ① $6 \times \frac{3}{2} = 9 > 6$

② $6 \times \frac{2}{3} = 4 < 6$

③ $6 \times 1 = 6 = 6$

Example

Which product is less than 6? Answer the letter of the correct math sentences.

(a) $6 \times \frac{8}{7}$ (b) $6 \times \frac{12}{13}$ (c) 6×1 (d) $6 \times 1 \frac{1}{5}$



Because the product is less than 6 which is also multiplicand, we must choose the formula whose multiplier is less than 1.

Answer (b)

1 Which product is less than 12? Answer the letter of the correct math sentences.

(a) $12 \times \frac{8}{9}$ (b) 12×1 (c) $12 \times \frac{7}{5}$ (d) $12 \times \frac{23}{25}$
(e) $12 \times 2 \frac{1}{3}$ (f) $12 \times \frac{11}{12}$

Answer _____

2 Which product is more than 31? Answer the letter of the correct math sentences.

(a) $31 \times \frac{5}{4}$ (b) $31 \times \frac{2}{3}$ (c) $31 \times 1 \frac{1}{10}$ (d) $31 \times \frac{32}{31}$
(e) 31×1 (f) $31 \times \frac{17}{18}$

Answer _____

5 - 13

How to Divide by Fractions

Size of the Quotient

Instruction In division, when the divisor is a whole number or decimal number, the size of the quotient and the size of the dividend are related in the following pattern:

- ① When divisor > 1 , quotient $<$ dividend
- ② When divisor < 1 , quotient $>$ dividend
- ③ When divisor $= 1$, quotient $=$ dividend

For example, ① $6 \div \frac{3}{2} = 4 < 6$

② $6 \div \frac{2}{3} = 9 > 6$

③ $6 \div 1 = 6 = 6$

Example Which quotient is more than 7? Answer the letter of correct math sentences.

(a) $7 \div 1 \frac{2}{9}$ (b) $7 \div 1$ (c) $7 \div \frac{9}{13}$ (d) $7 \div \frac{4}{3}$



Because the quotient is more than 7 (which is also dividend), we must choose the formula whose divisor is less than 1.

Answer (c)

1 Which quotient is less than 15? Answer the letter of correct math sentences.

(a) $15 \div \frac{5}{9}$ (b) $15 \div \frac{13}{12}$ (c) $15 \div \frac{19}{50}$ (d) $15 \div \frac{7}{5}$
(e) $15 \div 1 \frac{1}{2}$ (f) $15 \div 1$

Answer _____

2 Which quotient is more than 9? Answer the letter of correct math sentence.

(a) $9 \div \frac{3}{7}$ (b) $9 \div \frac{6}{5}$ (c) $9 \div 2 \frac{3}{4}$ (d) $9 \div 1$
(e) $9 \div \frac{11}{10}$ (f) $9 \div \frac{1}{34}$

Answer _____

5 - 14

How to Divide by Fractions

Review (1)

1 Calculate the following division problems. Simplify the answer. Leave them as improper fractions.

1 $\frac{3}{5} \div \frac{4}{7}$

2 $\frac{16}{25} \div \frac{12}{5}$

3 $2\frac{1}{6} \div 3\frac{1}{4}$

4 $3\frac{1}{3} \div 1\frac{3}{7}$

5 $18 \div 2\frac{2}{5}$

6 $\frac{7}{9} \div 14$

7 $0.6 \div \frac{2}{5}$

8 $1.8 \div 7\frac{1}{5}$

9 $\frac{3}{4} \times \frac{2}{5} \div \frac{15}{8}$

10 $4 \times \frac{5}{6} \div 0.8$

11 $\frac{8}{3} \div \frac{4}{9} \div 1.6$

12 $2.1 \div \frac{7}{8} \div 6$

2 Which product is more than 5? Answer the letter of correct math sentence.

(a) $5 \times 1\frac{1}{2}$ (b) $5 \times \frac{2}{3}$ (c) 5×1 (d) $5 \times \frac{17}{18}$

(e) $5 \times \frac{10}{7}$ (f) $5 \times \frac{6}{5}$

Answer _____

3 Which quotient is less than 8? Answer the letter of correct math sentence.

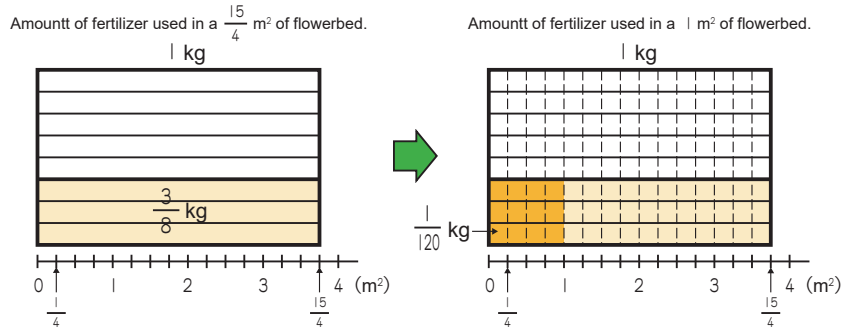
(a) $8 \div \frac{24}{25}$ (b) $8 \div \frac{4}{5}$ (c) $8 \div \frac{4}{3}$ (d) $8 \div 1\frac{1}{10}$

(e) $8 \div 1$ (f) $8 \div \frac{7}{8}$

Answer _____

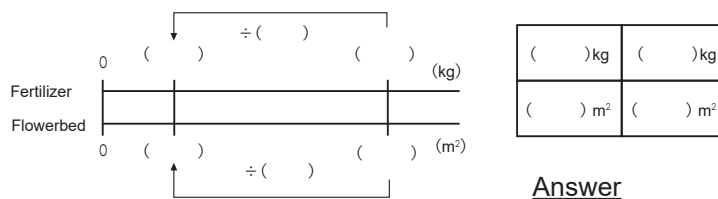
4 $\frac{3}{8}$ kg of fertilizer is used in a $\frac{15}{4}$ m² flowerbed. Answer the following questions.

1 How many kg of fertilizer do we need for an 1 m² of flowerbed?



Complete the number line diagrams and tables.

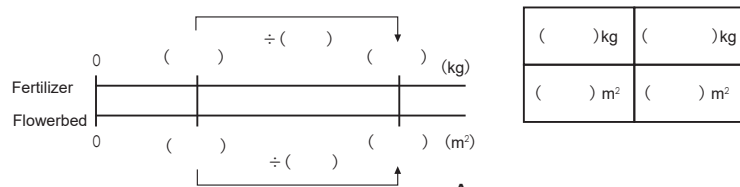
Math sentence



Answer _____

2 How many m² of flowerbed can be fertilized with 1 kg of fertilizer?

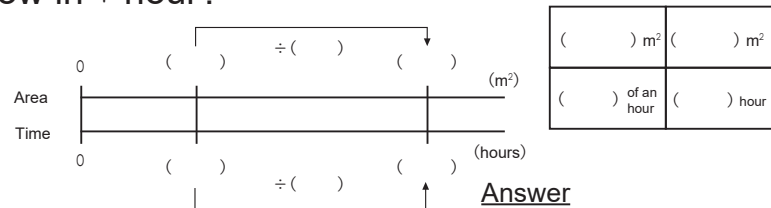
Math sentence



Answer _____

5 A lawnmower can mow 35 m² of grass in 20 minutes. How many m² of grass can this lawnmower mow in 1 hour?

Math sentence



Answer _____

6 Which of the following word problems equals the math sentence:

$\frac{1}{3} \div \frac{2}{5}$? Write the letter to the correct word problem.

- (a) We painted a $\frac{2}{5}$ m² of board with $\frac{1}{3}$ dL of paint. How many m² of board can we paint with 1 dL of this paint?
- (b) There is a rectangular piece of paper with an area of $\frac{1}{3}$ m². The length of the paper is $\frac{2}{5}$ m. How many m is the width of this paper?
- (c) There is oil that weighs $\frac{1}{3}$ kg per L. How much kg is $\frac{2}{5}$ L of this oil?

Answer _____

5 - 15

How to Divide by Fractions

Times as Much with Fractions (1)

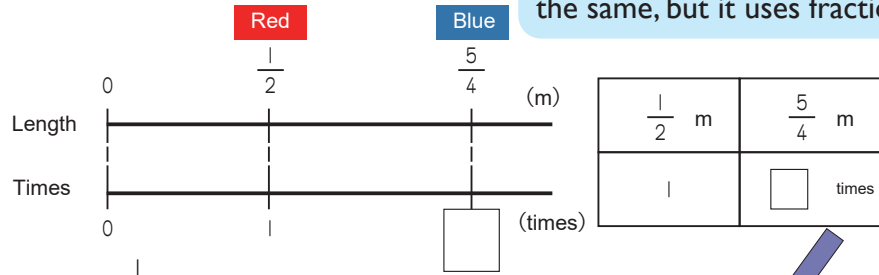
Example A blue ribbon is $\frac{5}{4}$ m. A red ribbon is $\frac{1}{2}$ m. How many times longer is the blue ribbon?



We can consider the length of the red ribbon as 1.

Once we draw a diagram, it is easier to understand.

If a red ribbon is 2 m and blue ribbon is 6 m, we can calculate it easily. This problem is also the same, but it uses fractions.



Math sentence

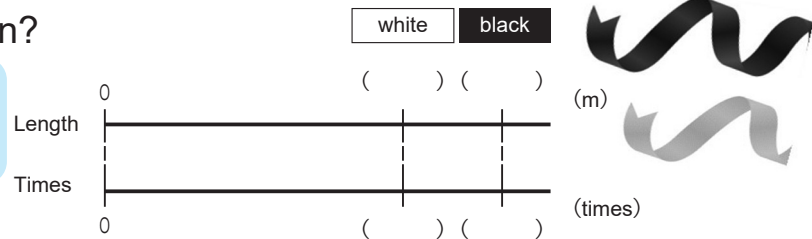
$$\frac{5}{4} \div \frac{1}{2} = \frac{5}{4} \times \frac{2}{1} = \frac{5 \times 2}{4 \times 1} = \frac{5}{2} \text{ or } 2 \frac{1}{2} \text{ Answer } \frac{5}{2} \text{ times or } 2 \frac{1}{2} \text{ times}$$

Even when fractions are involved, we use division to find out how many times as much something is as a base quantity.

1 A black ribbon is $\frac{2}{3}$ m. A white ribbon is $\frac{5}{9}$ m. How many times longer is the black ribbon?



Complete the number line diagrams and tables.

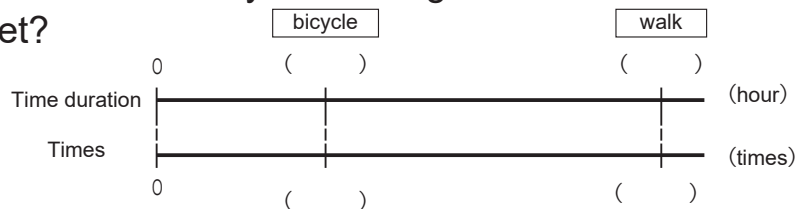


Math sentence

Answer

2 It takes $\frac{2}{7}$ of an hour to walk to the market. It takes $\frac{2}{25}$ of an hour to go to the market by bicycle. How many times longer does it take to walk than bicycle to the market?

Math sentence



Answer

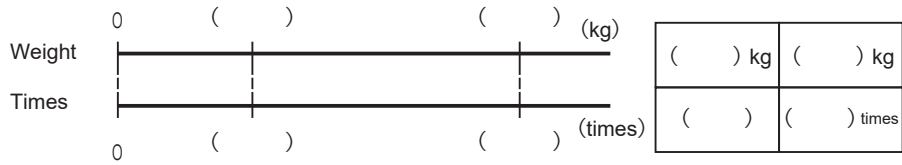
2 Answer the following questions.

1 How many times heavier is $\frac{5}{12}$ kg than $\frac{7}{6}$ kg?

Complete the number line diagrams and tables.



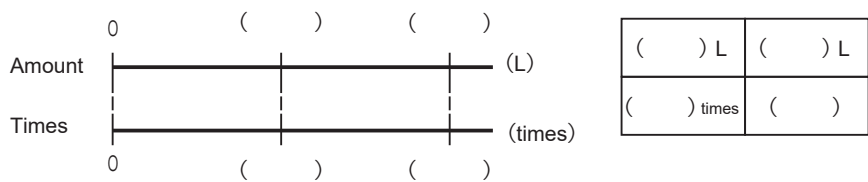
Math sentence



Answer

2 How many times more is $\frac{5}{12}$ L than $\frac{8}{9}$ L?

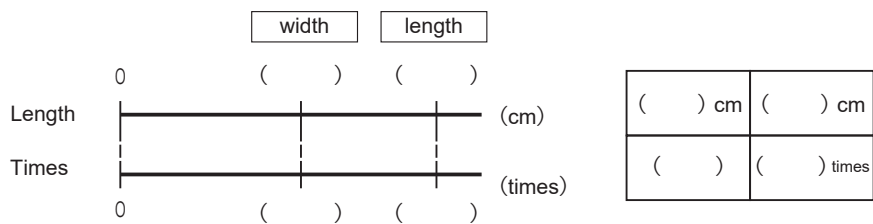
Math sentence



Answer

3 A rectangle piece of paper is $\frac{4}{3}$ cm long and $\frac{4}{5}$ cm wide. How many times longer is the length of the rectangle than the width?

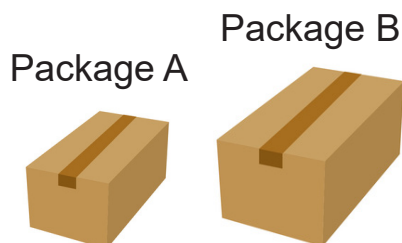
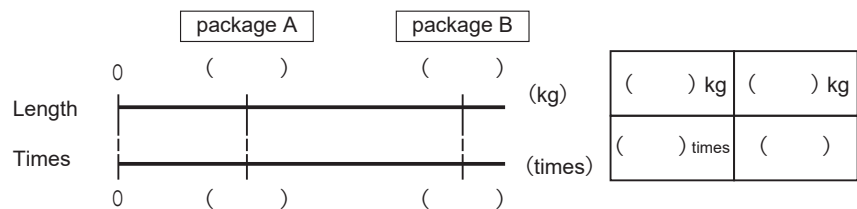
Math sentence



Answer

4 Package A weighs $\frac{3}{5}$ kg. Package B weighs $\frac{3}{2}$ kg. How many times heavier is Package A than Package B?

Math sentence



Answer

5 - 16

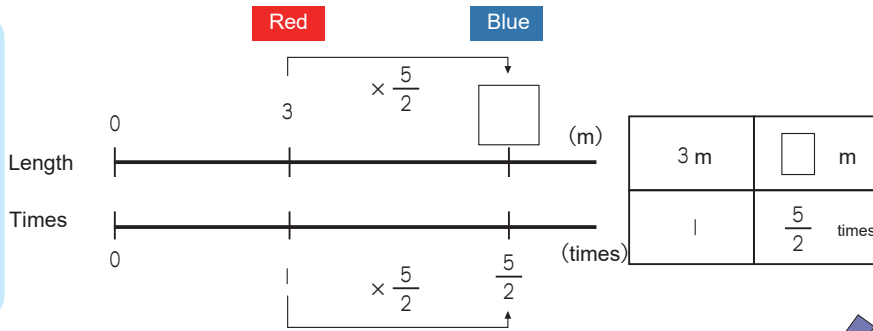
How to Divide by Fractions

Times as Much with Fractions (2)

Example A blue ribbon is $\frac{5}{2}$ times longer than the red ribbon. If the red ribbon is 3 m, how long is the blue ribbon?



Sometimes the word problem can be easier to understand if we use a whole number. If the blue ribbon is 2 times longer than the red ribbon, the blue ribbon is 6 m (3×2).



Math sentence

$$3 \times \frac{5}{2} = \frac{3 \times 5}{1 \times 2} = \frac{15}{2} \text{ or } 7 \frac{1}{2}$$

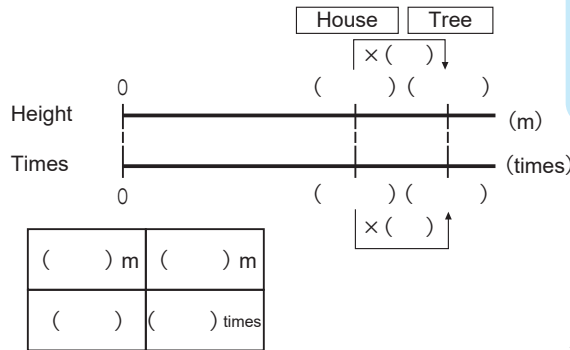
Answer $\frac{15}{2}$ m or $7 \frac{1}{2}$ m

Even when fractions are involved, we use multiplication to find out the amount to be compared. A formula is: (a base amount) \times (how many times as much)

1 The tree in front of my house is $\frac{4}{3}$ times taller than my house. If my house is 9 m tall, how tall is the tree?



Math sentence



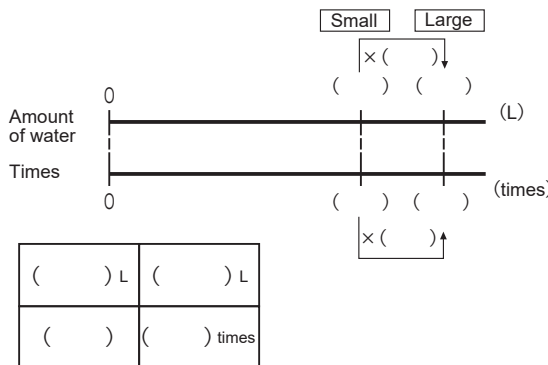
Complete the number line diagrams and tables.



Answer _____

2 A small water tank holds 50 L of water. A bigger water tank holds $\frac{6}{5}$ times as much water as the small tank. How much water can the bigger water tank hold?

Math sentence

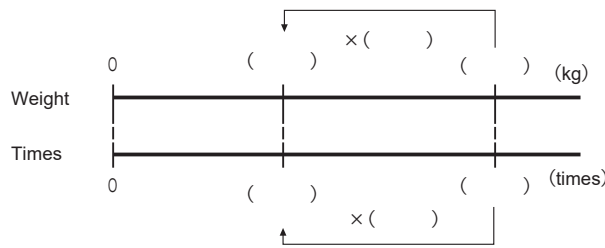


Answer _____

2 Answer the following questions.

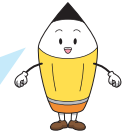
1 What is $\frac{3}{7}$ of 35 kg?

Math sentence



() kg	() kg
() times	()

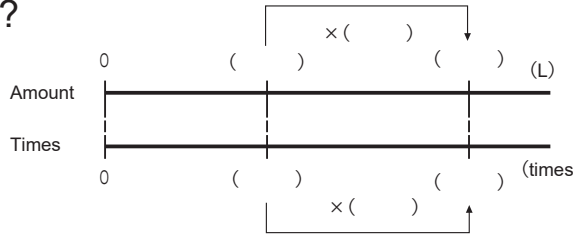
Complete the number line diagrams and tables.



Answer _____

2 What is $\frac{9}{4}$ of 20 L?

Math sentence

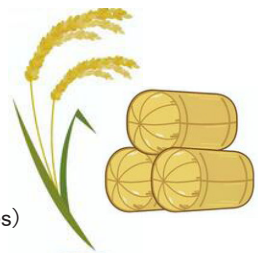
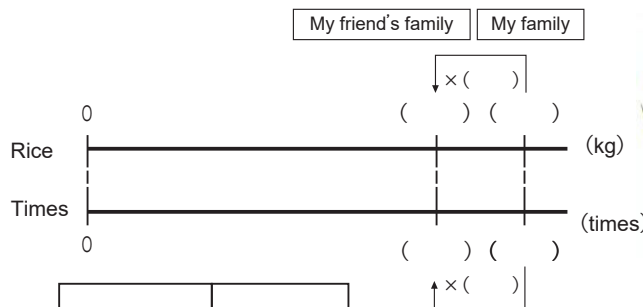


() L	() L
()	() times

Answer _____

3 My family consumes 25 kg of rice every month. My friend's family consumes $\frac{4}{5}$ as much. How much rice does my friend's family consume every month?

Math sentence

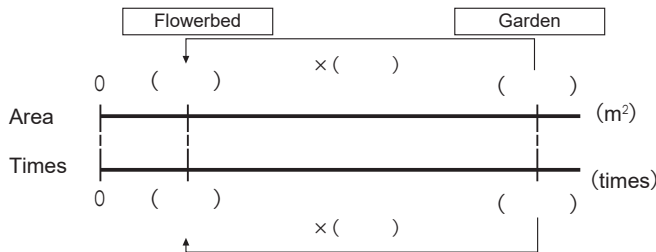


() kg	() kg
() times	()

Answer _____

4 The garden has an area of 240 m². The flowerbed's area is $\frac{3}{16}$ of the garden. What is the area of the flowerbed?

Math sentence



() m ²	() m ²
() times	()

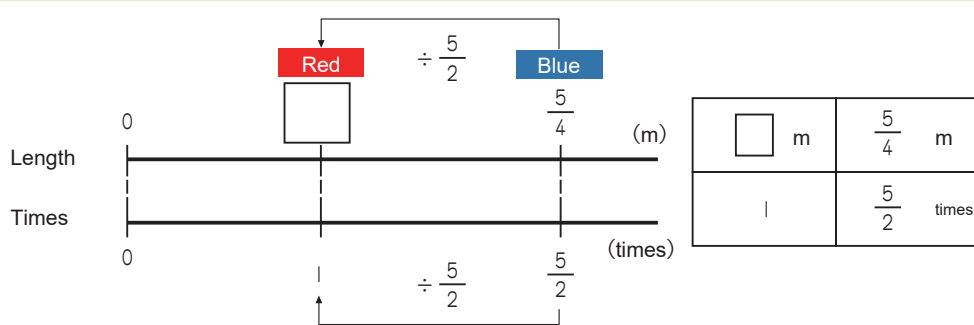
Answer _____

5 - 17

How to Divide by Fractions

Times as Much with Fractions (3)

Example A blue ribbon is $\frac{5}{2}$ times longer than the red ribbon. If the blue ribbon is $\frac{5}{4}$ m, how long is the red ribbon?



Sometimes the word problem can be easier to understand if we use a whole number. If the blue ribbon is 5 times longer, then divide $\frac{5}{4}$ (m) by 5.

Math sentence

$$\frac{5}{4} \div \frac{5}{2} = \frac{\cancel{5}}{4} \times \frac{2}{\cancel{5}} = \frac{1}{2}$$

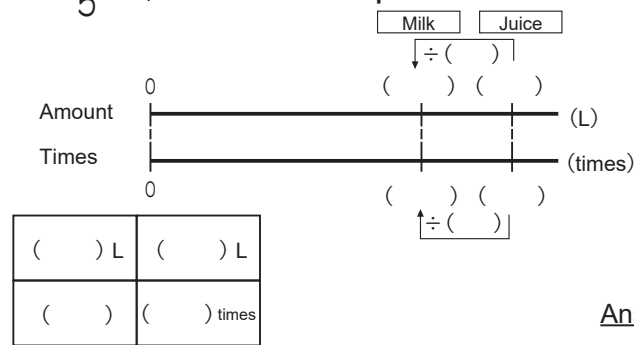
Answer $\frac{1}{2}$ m

Even when fractions are involved, we use division to find out the amount to be a base. A formula is: (amount to be compared) \div (how many times as much)

1 A juice bottle can hold $\frac{4}{3}$ times more liquid than a milk bottle. If the juice bottle can hold $\frac{6}{5}$ L, how much liquid can a milk bottle hold?



Math sentence

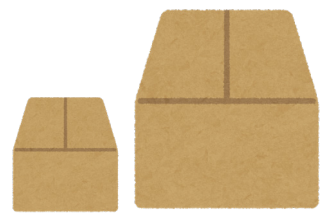
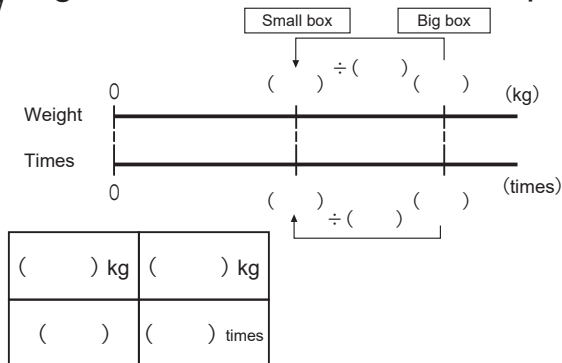


Complete the number line diagrams and tables.

Answer _____

2 A big package is $\frac{5}{3}$ times heavier than a small package. If the big package weighs $\frac{8}{9}$ kg, how much does the small package weigh?

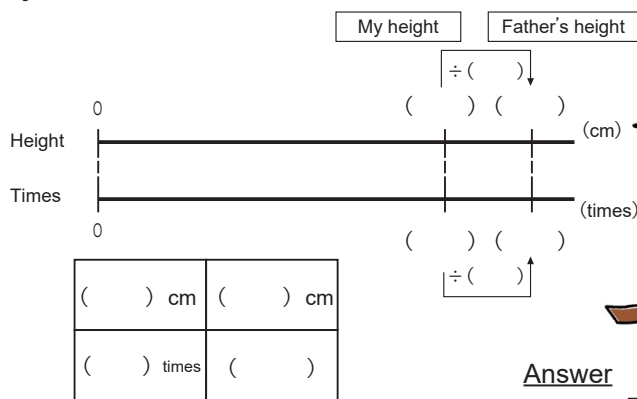
Math sentence



Answer _____

3 I am $\frac{4}{5}$ as tall as my father. If I am 140 cm tall, how tall is my father?

Math sentence

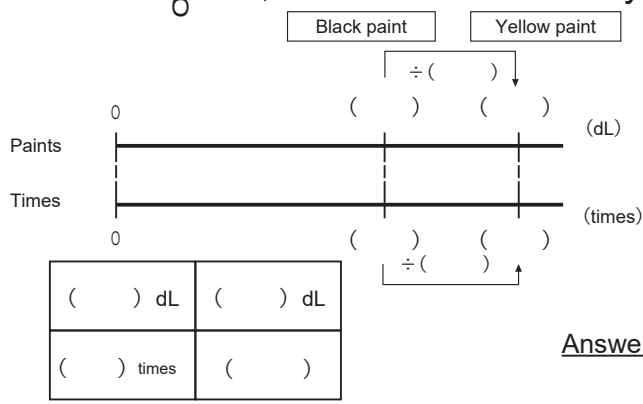


Complete the number line diagrams and tables.

Answer _____

4 The can of black paint holds $\frac{2}{3}$ as much as the can of yellow paint. If the can of black paint holds $\frac{25}{6}$ dL, how much does the yellow paint can hold?

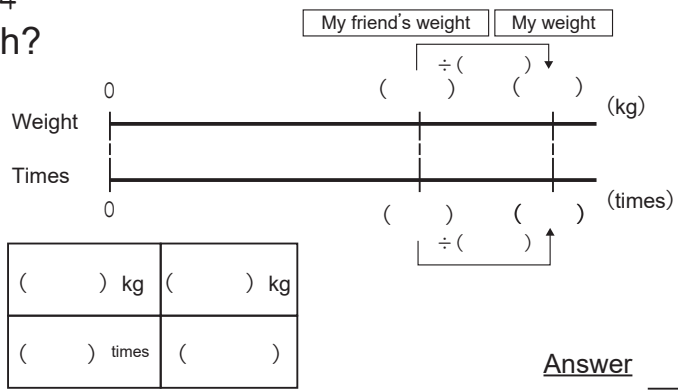
Math sentence



Answer _____

5 My classmate is $\frac{3}{4}$ as heavy as mine. If my classmate weighs 42 kg, How much do I weigh?

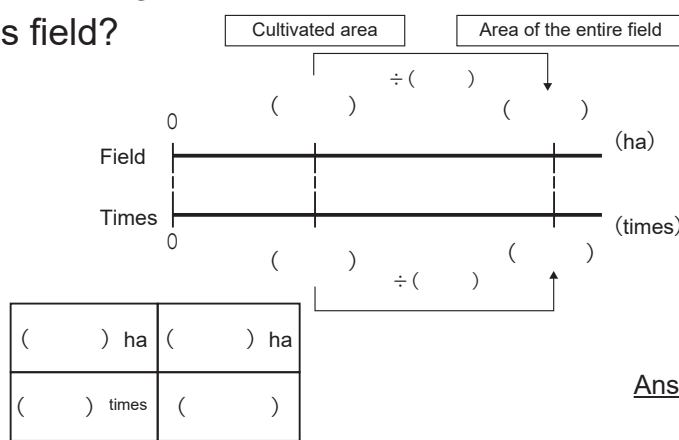
Math sentence



Answer _____

6 A farmer cultivated $\frac{3}{8}$ of his field. If the farmer cultivated $\frac{1}{6}$ ha, what is the size of his field?

Math sentence



Answer _____

5 - 18

How to Divide by Fractions

Review (2)

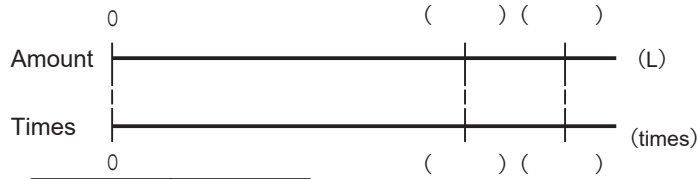
1 Calculate the following.

1 2 times of $\frac{3}{7}$ m m 2 $\frac{6}{5}$ times of $\frac{3}{4}$ m m

3 $\frac{2}{3}$ times of $\frac{9}{8}$ m m 4 $\frac{16}{15}$ times of $\frac{5}{8}$ m m

2 How many times more L is $\frac{13}{15}$ L than $\frac{4}{5}$ L?

Math sentence



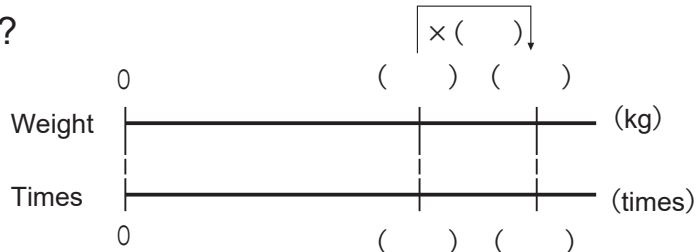
() L	() L
()	() times

Answer _____

Complete the number line diagrams and tables.

3 What is $\frac{7}{5}$ of 20 kg?

Math sentence

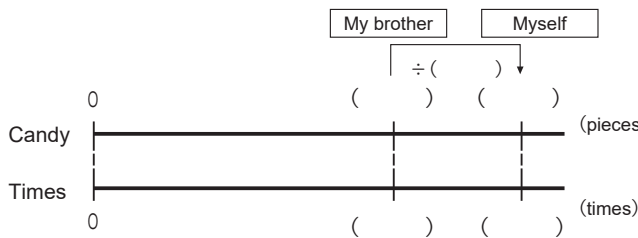


() kg	() kg
()	() times

Answer _____

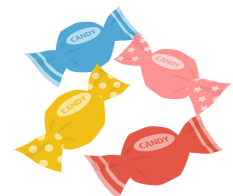
4 My brother has $\frac{3}{4}$ as many pieces of candy as I have. If my brother has 12 pieces of candy, how many do I have?

Math sentence



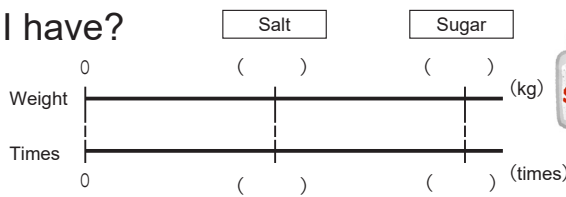
() pieces	() pieces
() times	()

Answer _____



5 I have $\frac{8}{5}$ kg of sugar and $\frac{3}{4}$ kg of salt. How many times more kg of sugar than salt do I have?

Math sentence



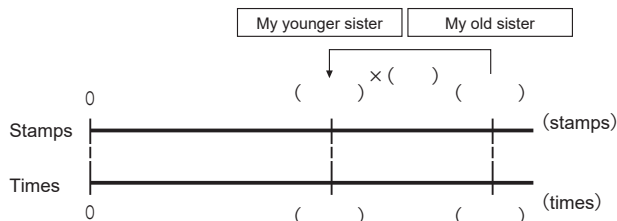
Complete the number line diagrams and tables.

() kg	() kg
() times	() times

Answer _____

6 My younger sister has $\frac{3}{5}$ as many as stamps as my older sister. If my older sister has 75 stamps, how many stamps does my younger sister have?

Math sentence

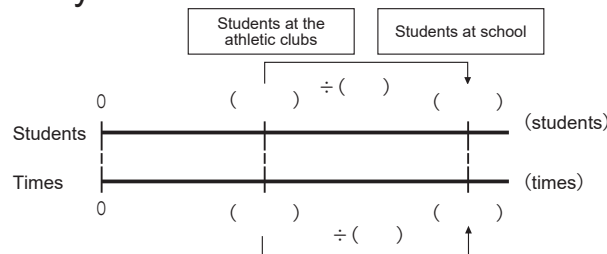


() stamps	() stamps
() times	()

Answer _____

7 $\frac{4}{9}$ of the students at school participate in athletic clubs. If 100 students in athletic clubs, how many students are there at school?

Math sentence

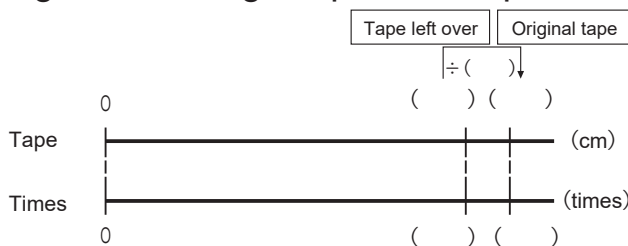


() students	() students
() times	()

Answer _____

8 I used $\frac{1}{9}$ of a piece of tape. The amount of tape left over is 160 cm long. What was the length of the original piece of tape?

Math sentence



To solve this question, calculate how much tape I used.

() cm	() cm
() times	()

Answer _____