## HOW TO PREPARE FOR COLUMN METHOD IN FOUNDATION PHASE

- Prepare our learners for fundamental skills of calculation -

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## Introduction

- $79.5 \%$ in grade 5 and $60.3 \%$ in grade 7 learners rely on unit counting (Schollar. 2008)

We need to let learners move away from unit-counting in addition and subtraction.

We propose the following methods to understand base-ten number system conceptually:

- Subitising
- Make-a-ten method
- Column method


## Outline of today's activity

We do the following activities today.

| Agenda | Contents | puration |
| :---: | :---: | :---: |
| Introduction | What is necessary for four basic operations in the - Make-a-ten method? | 0 minutes |
| Activity 1 (hands-on) | In activity 1, we do: <br> - instant recognition of numbers up to 10 using a ten-frame; and <br> - calculation with bottle tops and ten-frames using the make-a-ten method. <br> - Column method | 15 minutes |
| Activity 2 (hands-on) | In activity 2, we calculate with: <br> - printed tens and hundreds <br> - printed tens and bottle tops; and <br> - column method. | 5 minutes |
| Discussion/Feedback | What advantages and disadvantages did the participants find? | 10 minutes |
| Wrap up | Conclude the workshop. | 5 minutes |

## Basic Knowledge and skills for Activity 1-1

We use subitising with a ten-frame.

## What is subitising?

Subitising is the instant recognition of the number of objects in a collection without counting them.

## What is a ten-frame?

A ten-frame is a frame showing 10 boxes. Each of the box holds a bottle top.


## Basic Knowledge and skills for Activity 1-1

Can we know the number of dots without counting?


This thick line shows 5.
The answer is 9 .

## Base-ten kit

The following is the components of base-ten kit.

| Tens | Ones |
| :---: | :---: |
|  |  |
|  |  |
|  |  |
|  |  |
| Tens |  |
|  |  |

Place-value table


Hundreds


Tens


Ten-frames


Bottle tops

## Activity 1-1 (3 minutes)

<Tool>
10 bottle tops and a ten-frame.
<Steps>Work in pairs.

1. One of the participants take bottle tops (any number).
2. The other participants answer how many without counting them.
3. Check the answer by placing them in a ten-frame.
4. Repeat 1-3 by turn.

## Addition and subtraction

Addition and subtraction up to 20 are divided into the following types.

| Type | Addition | Subtraction |
| :---: | :---: | :---: |
| Without carrying or borrowing | $\begin{aligned} & \text { (1-digit) }+(1 \text {-digit })<10 \\ & \text { e.g. } 2+4=6 \end{aligned}$ | $\begin{aligned} & \text { (1-digit) - (1-digit) } \\ & \text { e.g. } 5-3=2 \end{aligned}$ |
|  | $\begin{aligned} & \text { (numbers 10-18) }+(1 \text {-digit })<20 \\ & \text { e.g. } 12+4=16 \end{aligned}$ | $\begin{aligned} & \text { (number } 11-18)-(1-\text { digit }) \geqq 10 \\ & \text { e.g. } 15-3 \end{aligned}$ |
| With carrying and borrowing | $\begin{aligned} & \text { (1-digit) }+(1 \text {-digit }) \geqq 10 \\ & \text { e.g. } 9+4 \end{aligned}$ | $\begin{aligned} & \text { (number 11-18) }-(1 \text {-digit })<10 \\ & \text { e.g. } 15-9 \end{aligned}$ |
|  |  | e inverse operations. |

## Without carrying or borrowing (1-digit)

(1-digit) $+(1$-digit $)<10$ and its inverse.


## Activity 1-2 (5 minutes)

## <Tool>

Bottle tops with 2 ten-frames.
<Steps> Work in pairs.

1. Solve the following using a base-ten kit.

- $12+4$
- 15-3

2. Solve the following using a base-ten kit.

- $9+4$
- 15-9

3. Find the difference between 1 and 2 .

## Without carrying or borrowing (1-digit)

(numbers 10-18) + (1-digit) $<20$ and its inverse.


No change in a ten.


## Addition with carrying (Make-a-ten Method)

$$
9+4=13
$$

Number bonds of 10


Making a ten.

Move a bottle top

Number bonds of 4


## Subtraction with borrowing (Make-a-ten Method )

Remove 9 counters ${ }^{15-9=6}$


## Summary of Activity 1-2

1. No change in a ten.

- $12+4$ (addition without carrying)
- 15-3 (subtraction without borrowing)

2. Making a ten.

- $9+4$ (addition with carrying)
- 15-9 (subtraction with borrowing)


## Basic Knowledge and skills for Activity 2

We will work on (2-digit number) $\pm$ (2-digit number) with a base-ten kit as well as the column method.

We use printed tens and hundreds.
a printed ten

a printed hundred


## How to organise tens and hundreds better

(1) How many?

(2) How many?



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## How to organise tens and hundreds better

(1) How many?


5 tens and 3 tens make 8 tens
(2) How many?


| $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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Organise tens and hundreds in groups of 5 . This will help you subitise numbers.

## Activity 2-1 (3 minutes)

## <Tool>

10 printed tens and 2 printed hundreds.
<Steps> Work in pairs.
Solve the following using a base-ten kit.

1. $40+30$
2. $80-20$
3. $110+40$
4. $240-100$

## Activity 2-1

1. $40+30=70$

|  |  |
| :---: | :---: |
|  |  |

3. $110+40=150$

4. $80-20=60$

5. $240-100=140$


## Column method

Four basic operations are the foundation of numbers and operations.

We recommend the column method for the four basic operation because:

- Algorithm is simple;
- It represents base-ten number system;
- It is all-round; and
- It is universal method of calculation.

When the sum exceeds ten, the ten is carried to the next place.
$3 \begin{array}{lll}1 & 1 & 1 \\ 4 & 876\end{array}$
$+43875$
78751

## Column method

We recommend introducing the column method for the four basic operation in early grade. Why the column method in early grade?

Because:

- it is easy to learn in small number; and
- learners have readiness for it.


## Column method

Addition and subtraction in columns are the keys to learning the four operations.
Why the column method of addition and subtraction is critical?

The column method
of multiplication


1972

The long division


Because they are used in the column method of multiplication and long division.

## Activity 2-2 (5 minutes)

## <Tool>

5 printed tens and 15 bottle tops.
<Steps> Work in pairs.
Solve the following using a base-ten kit.

1. $28+14$
2. 53-26

Activity 2-2 (28+14)

28



Activity 2-2 (53-26)

| Tens |  |  | Ones |
| :---: | :---: | :---: | :---: |
| $\bullet$ | - $\cdot$ |  |  |
| $\bullet$ | - | $\bullet$ |  |
| - | - $\cdot \bullet$ |  |  |
| $\bullet$ | - | $\bullet$ |  |
| - | - $\bullet$ | $\bullet$ |  |
| $\bullet$ | $\bullet$ | $\bullet$ |  |
| - | - $\cdot$ - | $\bullet$ |  |
| - | - $\cdot$ |  | $\bullet$ |
| $\bullet$ | - | - | $\bullet$ |
| $\bullet$ | - - |  | $\bullet$ |
|  | 2 ten |  | 7 ones |
|  |  | 27 |  |

$\left.\begin{array}{c|c|}\mathbf{T} & 0 \\ 4 & 1 \\ \hline 5 & 3 \\ - & 2\end{array}\right)$

## Wrap up

- Using a base-ten kit helps learners move away from counting.
- Showing learners steps of the column method using a base-ten kit.
- Addition and subtraction up to 20 are crucial, which will be used in higher grades repeatedly. (See the next slide)


## Importance of addition and subtraction up to 20 [1]



2 ones + 3 ones

2 tens +3 tens


2 hundreds +3 hundreds


2 tenths +3 tenths

$$
(0,1+0,1)+(0,1+0,1+0,1)
$$

## 2 sixths +3 sixths

$$
\left(\frac{1}{6}+\frac{1}{6}\right)+\left(\frac{1}{6}+\frac{1}{6}+\frac{1}{6}\right)
$$

Addition and subtraction up to 20 are important

## Importance of addition and subtraction up to 20 [2]

How many types of additions involves carrying?

|  | Without carrying <br> (patterns) | With carrying <br> (patterns) | With carrying <br> (\%) |
| :--- | :---: | :---: | :---: |
| (1-digit) + (1-digit) | 55 | 45 | $45 \%$ |
| (2-digit) + (2-digit)* | 3025 | 6975 | $69,8 \%$ |
| (3-digit) + (3-digit)* | 166375 | 833625 | $83.4 \%$ |

The more number increases, the more patterns of addition involve carrying.

[^0]
## Bad Practices in TMU pilot

<Examples of Bad Practice>
Some teachers:

- counted bottle tops in a ten-frame. Bear in mind that the thick line means 5.
- let learners count bottle tops. Avoid counting as much as possible;
- did not organise tens and hundreds. Organise in groups of 5.

Always make groups of 5, 10, 100 etc.
This will help learners understand numbers as a group.

## Thank you so much！！

ありがとうございました！

Arigato gozai masita．


[^0]:    * (2-digit) + (2-digit) includes (2-digit) + (1-digit), (1-digit) + (2-digit) and (1-digit) + (1-digit)

